## **Automated Theorem Proving**

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## **Exercises 14: Efficient Saturation Procedures and Outlook**

Exercise 14.1: Consider the following path index:



Does path index contain the terms  $t_1 = g(h(d), h(*)), t_2 = g(h(b), c), t_3 = g(*, *)$ ? If yes, what are their numbers in the index?

Exercise 14.2: Consider the following path index:



(a) Which terms have the numbers 3, 5, and 12 in the path index?

(b) Which of the terms g(\*, h(\*)), f(g(d, c)), and g(h(\*), c) are contained in the path index? If they are contained, what are their numbers?

(c) Assume that the terms in the path index are the left-hand sides of the rewrite rules of a TRS R. Is the term f(g(h(d), f(c))) reducible by rules in R? If yes, what are the numbers of the left-hand sides of these rules?

**Exercise 14.3:** Could one use the following numbers as features in a feature vector index?

- (1) the number of ground arguments of predicate symbols in a clause,
- (2) the number of variable occurrences in a clause,
- (3) the number of constant symbols occurring in positive literals in a clause,
- (4) the number of literals in a clause that do not contain variables,
- (5) the number of literals in a clause that do not contain the function symbol f,
- (6) the number of literals in a clause that do not contain the predicate symbol P,
- (7) the number of literals in a clause that contain neither variables nor the function symbol f,
- (8) the number of distinct variables in a clause.